

AP Calculus AB
Unit 2 - Differentiation
2.2C - PDFs and Differentiability

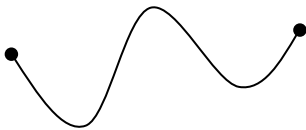
$f(x)$ is differentiable at a **left end-point** at $x = a$ if:

- i) $f(x)$ is continuous from the right.
- ii) $\lim_{h \rightarrow a^+} \frac{f(a+h) - f(a)}{h}$ exists.

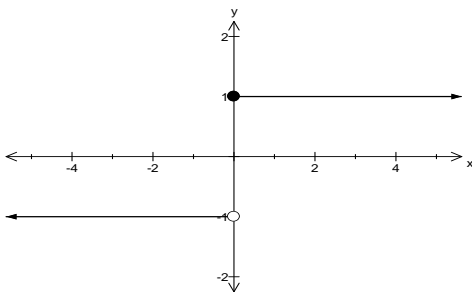
$f(x)$ is differentiable at a **right end-point** at $x = a$ if:

- i) $f(x)$ is continuous from the left.
- ii) $\lim_{h \rightarrow a^-} \frac{f(a+h) - f(a)}{h}$ exists.

e.g.



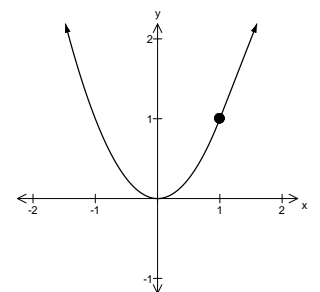
1. Consider the graph of $f(x)$ given below:



Is $f(x)$ left-hand differentiable at $x = 0$?

Is $f(x)$ right-hand differentiable at $x = 0$?

2. Consider $f(x) = \begin{cases} x^2 & ; x \leq 1 \\ 2x-1 & ; x > 1 \end{cases}$ Is $f(x)$ differentiable at $x = 1$?



Check continuity at $x = 1$:

Check left-hand derivative at $x = 1$:

Check right-hand derivative at $x = 1$:

3. Consider $f(x) = \begin{cases} x^2 + x; & x \leq 1 \\ 3x - 2; & x > 1 \end{cases}$ Is $f(x)$ differentiable at $x = 1$?

4. Consider $f(x) = \begin{cases} ax^2 - 2x; & x \leq 2 \\ 4x + 2b; & x > 2 \end{cases}$ Determine the values of a and b that make $f(x)$ differentiable at $x = 2$.